# Parallel and Distributed Algorithms

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## Assignment 9

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Problem 9.3 provides eight *extra* credit points. Thus, there are 32 points achievable on this assignment, but only 24 points are accounted for as 100%.

#### 9.1. Problem (12)

Dijkstra's Token Termination Detection Algorithm II

Consider Dijkstra's Token Termination Detection Algorithm II. All messages are guaranteed to be *non–overtaking*. That is, if a process sends two messages  $M_1$  and  $M_2$  to another process,  $M_1$  is received before  $M_2$ .

- a.) Prove the correctness of Dijkstra's Token Termination Detection Algorithm II.
- b.) Does it suffice in step (2) that a process *i* is colored black only if it sends a message to a process *j* with j < i?
- c.) Does it suffice in step (2) that a process i is colored black only if it sends a message?

### **9.2. Problem (12)**

More on Termination Detection

Here are three more procedures to detect termination. Are they correct? You may assume that messages are delivered *in order*.

- a.) Process 1 inserts a token into the process ring. A process keeps the token as long as it has work to do and passes it along otherwise. Process 1 prepares the shutdown whenever receiving the token from process *p*.
- b.) Process 1 inserts a white token into the process ring. A process colors the token black if it has work to do and passes it along. An idle process passes the token along without changing its color. Process 1 prepares the shutdown whenever receiving a white token from process *p*.
- c.) Our last procedure works exactly as Dijkstra's Token Termination Detection Algorithm I, however whenever a token is passed to an active process, this process colors the token black and passes it on immediately.

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### **9.3. Problem (8)**

#### Early Termination Detection

a.) The weight procedure for termination detection in dynamic load balancing has to be modified to allow early termination when a process finds a solution. How should that be done?

b.) Does the implementation of Dijkstra's algorithm have to be modified?